Proposed problem

Determine the maximum and the minimum of $\sqrt{4 + 2x^2} + \sqrt{54 - 36\sqrt{2} + 4y^2}$ where $x, y \geq 0$, $x + y = 1$.